## Eighth Grade Math Scope and Sequence

|  | Quarter 1 | Quarter 2 | Quarter 3 | Quarter 4 |
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| Domain | Equations and Expressions Number System | Equations and Expressions Functions | Geometry | Statistics and Probability |
| THE NUMBER SYSTEM 8.NS <br> 1-2) Know that there are numbers that are not rational, and approximate them by rational numbers. <br> EXPRESSIONS AND EQUATIONS <br> 8.EE <br> 1-4) Work with radicals and integer exponents. 5-6) Understand the connections between proportional relationships, lines, and linear equations. 7-8) Analyze and solve linear equations and pairs of simultaneous linear equations. <br> FUNCTIONS $8 . F$ <br> 1-3) Define, evaluate, and compare functions. <br> 4-5) Use functions to model relationships between quantities. | 8.EE. 1 Understand, explain, and <br> apply the properties of integer exponents to generate equivalent numerical expressions. For example, $3^{2} \times$ $3-5=3-3=1 / 3^{3}=1 / 27$. <br> 8.EE. 2 Use square root and cube root symbols to represent solutions to equations of the form $x^{2}=p$ and $x^{3}=p$, where $p$ is a positive rational number. Evaluate square roots of small perfect squares and cube roots of small perfect cubes. Know that $\sqrt{ } 2$ is irrational. <br> 8.EE. 3 Use numbers expressed in the form of a single digit times an integer power of 10 to estimate very large or very small quantities and to express how many times as much one is than the other. For example, estimate the population of the United States as $3 \times 108$; and the population of the world as $7 \times$ 109; and determine that the world population is more than 20 times larger. <br> 8.EE. 4 Perform operations with numbers expressed in scientific notation, including problems where both decimal notation and scientific notation are used. Use scientific notation and choose | 8.EE. 5 Graph proportional relationships, interpreting the unit rate as the slope of the graph Compare two different proportional relationships represented in different ways. For example, compare a distancetime graph to a distance-time equation to determine which of two moving objects has greater speed. <br> 8.EE. 6 Use similar triangles to explain why the slope $m$ is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation $y=m x$ for a line through the origin and the equation $y=$ $m x+b$ for a line intercepting the vertical axis at $b$. <br> 8.F. 1 Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output. Function notation is not required in Grade 8. <br> 8.F. 2 Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). Fo example, given a linear function | 8.EE.8 Analyze and solve pairs <br> of simultaneous linear equations graphically. <br> 8a. Understand that the <br> solution to a pair of linear equations in two variables corresponds to the point(s) of intersection of their graphs, because the point(s) of intersection satisfy both equations simultaneously. 8b. Use graphs to find or estimate the solution to a pair of two simultaneous linear equations in two variables. Equations should include all three solution types: one solution, no solution, and infinitely many solutions. Solve simple cases by inspection. For example, $3 x+2 y=5$ and $3 x+$ $2 y=6$ have no solution because $3 x+2 y$ cannot simultaneously be 5 and 6 . 8c. Solve real-world and mathematical problems leading to pairs of linear equations in two variables. For example, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair. (Limit solutions to those that can be addressed by graphing.) <br> 8.G. 1 Verify experimentally the | 8.G.6-8 Continued <br> 8.G.9 Solve real-world and mathematical problems involving volumes of cones, cylinders, and spheres. <br> 8.SP. 1 Construct and interpret scatter plots for bivariate G measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering; outliers; positive, negative, or no association; and linear association and nonlinear association. (GAISE Model, steps 3 and 4) <br> 8.SP. 2 Understand that straight lines are widely used to model relationships between two quantitative variables. For scatter plots that suggest a linear association, informally fit a straight line, and informally assess the model fit by judging the closeness of the data points to the line. (GAISE Model, steps 3 and 4) <br> 8.SP. 3 Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. For example, in a linear model for a biology experiment, interpret a slope of $1.5 \mathrm{~cm} / \mathrm{hr}$ as meaning that |

## GEOMETRY

1-5) Understand congruence and similarity using physical models, transparencies, or geometry software. 6-8) Understand and apply the Pythagorean Theorem
9) Solve real-world and mathematical problems involving volume of cylinders, cones, and spheres.

## STATISTICS AND PROBABILITY

## 8.SP

1-4) Investigate patterns of association in bivariate data.
measurements of very large or very small quantities, e.g., use millimeters per year for seafloor spreading. Interpret scientific notation that has been generated by technology.
8.NS. 1 Know that real numbers are either rational or irrational. Understand informally that every number has a decimal expansion which is repeating, terminating, or is non-repeating and non-terminating.
8.NS. 2 Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions, e.g., $\pi^{2}$. For example, by truncating the decimal expansion of $\sqrt{ } 2$, show that $\sqrt{ } 2$ is between 1 and 2 , then between 1.4 and 1.5 , and explain how to continue on to get better approximations
8.EE. 7 Solve linear equations in one variable.
7a. Give examples of linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms, until an equivalent equation of the form $x=a, a=a$, or $a=b$ results (where a and b are different numbers).
7b. Solve linear equations with rational number coefficients,
and a linear function represented by an algebraic expression, determine which function has the greater rate of change.
8.F. 3 Interpret the equation $y=$ $m x+b$ as defining a linear function, whose graph is a straight line; give examples of functions that are not linear. For example, the function $\mathrm{A}=\mathrm{s}^{2}$ giving the area of a square as a function of its side length is not linear because its graph contains the points $(1,1),(2,4)$ and $(3,9)$, which are not on a straight line.
8.F. 4 Construct a function to model a linear relationship between two quantities.
Determine the rate of change and initial value of the function from a description of a relationship or from two ( $\mathrm{x}, \mathrm{y}$ ) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values.
8.F. 5 Describe qualitatively the functional relationship between two quantities by analyzing a graph, e.g., where the function is increasing or decreasing, linear or nonlinear. Sketch a graph that exhibits the qualitative features of a function that has been described verbally.
reflections, and translations (include examples both with and without coordinates). 1a. Lines are taken to lines, and line segments are taken to line segments of the same length. 1b. Angles are taken to angles of the same measure.
1c. Parallel lines are taken to parallel lines.
8.G. 2 Understand that a twodimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them. (Include examples both with and without coordinates.)
8.G. 3 Describe the effect of dilations, translations, rotations, and reflections on twodimensional figures using coordinates.
8.G. 4 Understand that a twodimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar twodimensional figures, describe a sequence that exhibits the similarity between them. (Include examples both with and without coordinates.)
8.G. 5 Use informal arguments to establish facts about the
day is associated with an additional 1.5 cm in mature plant height. (GAISE Model, steps 3 and
4)
8.SP. 4 Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables. For example, collect data from students in your class on whether or not they have a curfew on school nights and whether or not they have assigned chores at home. Is there evidence that those who have a curfew also tend to have chores?

|  | including equations whose solutions require expanding expressions using the distributive property and collecting like terms. |  | angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles. For example, arrange three copies of the same triangle so that the sum of the three angles appears to form a line, and give an argument in terms of transversals why this is so. <br> 8.G. 6 Analyze and justify an informal proof of the Pythagorean Theorem and its converse. <br> 8.G.7 Apply the Pythagorean Theorem to determine unknown side lengths in right triangles in real-world and mathematical problems in two and three dimensions. <br> 8.G.8 Apply the Pythagorean Theorem to find the distance between two points in a coordinate system. |  |
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| Resources | Reveal Math <br> Modules 1, 2, 3 <br> ODE Model Curriculum GAISE model framework | Reveal Math Modules 4, 5 ODE Model Curriculum GAISE model framework | Reveal Math Modules 6, 7, 8, 9 ODE Model Curriculum GAISE model framework | Reveal Math Modules 7, 10, 11 ODE Model Curriculum GAISE model framework |

## CRITICAL AREAS

Critical Area 1: Formulating and reasoning about expressions and equations, including modeling an association in bivariate data with a linear equation, and solving linear equations and systems of linear equations
Students use linear equations and systems of linear equations to represent, analyze, and solve a variety of problems. Students recognize equations for proportions $(y / x=m$ or $y=m x)$ as special linear equations $(y=m x+b)$, understanding that the constant of proportionality ( $m$ ) is the slope, and the graphs are lines through the origin. They understand that the slope $(\mathrm{m})$ of a line is a constant rate of change so that if the input or x-coordinate changes by an amount $A$, the output or $y$-coordinate changes by the amount $m \cdot A$. Students also use a linear equation to describe the association between two quantities in bivariate data (such as arm span vs. height for students in a classroom). At this grade, fitting the model, and assessing its fit to the data are done informally.

Interpreting the model in the context of the data requires students to express a relationship between the two quantities in question and to interpret components of the relationship (such as slope and y-intercept) in terms of the situation.
Students strategically choose and efficiently implement procedures to solve linear equations in one variable, understanding that when they use the properties of equality and the concept of logical equivalence, they maintain the solutions of the original equation. Students solve systems of two linear equations in two variables graphically or by simple inspection; these intersect, are parallel, or are the same line. Students use linear equations, systems of linear equations, linear functions, and their understanding of slope of a line to analyze situations and solve problems.
Critical Area 2: Grasping the concept of a function and using functions to describe quantitative relationships
Students grasp the concept of a function as a rule that assigns to each input exactly one output. They understand that functions describe situations where one quantity determines another. They can translate among representations and partial representations of functions (noting that tabular and graphical representations may be partial representations), and they describe how aspects of the function are reflected in the different representations.

## Critical Area 3: Analyzing two- and three-dimensional space and figures using distance, angle, similarity, and congruence, and understanding

 and applying the Pythagorean TheoremStudents use ideas about distance and angles, how they behave under translations, rotations, reflections, and dilations, and ideas about congruence and similarity to describe and analyze two-dimensional figures and to solve problems. Students show that the sum of the angles in a triangle is the angle formed by a straight line, and that various configurations of lines give rise to similar triangles because of the angles created when a transversal cuts parallel lines. Students understand the statement of the Pythagorean Theorem and its converse, and can explain why the Pythagorean Theorem holds, for example, by decomposing a square in two different ways. They apply the Pythagorean Theorem to find distances between points on the coordinate plane, to find lengths, and to analyze polygons. Students complete their work on volume by solving problems involving cones, cylinders, and spheres.
Critical Area 4: Working with irrational numbers, integer exponents, and scientific notation
Students explore irrational numbers and their approximations. They extend work with expressions and equations with integer exponents, square and cube roots. Understandings of very large and very small numbers, the place value system, and exponents are combined in representations and computations with scientific notation.

